



*B-Physics Results  
from the  
Fermilab Tevatron*

P. Gutierrez

[gut@fnal.gov](mailto:gut@fnal.gov)

Homer L. Dodge Department of Physics & Astronomy  
University of Oklahoma

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# Tevatron *B*-Physics—Overview



## ⑥ Run II *B*-Physics results

- △ Lifetime ( $B^+$ ,  $B_d^0$ ,  $B_s^0$ ,  $B_c^+$ ,  $\Lambda_B$ , ...) measurements
- △ Mixing ( $B_d^0$ ,  $B_s^0$ ) measurements
- △ Branching ratios ( $B_{(s)}^0 \rightarrow \mu^+ \mu^- X$ ,  $B_s^0 \rightarrow D_s \bar{D}_s \dots$ )
- △ Spectroscopy ( $B_c$ ,  $B_1$ ,  $B_2^*$ ,  $B_{s2}^{*0}$ , ...)
- △ Production properties (cross sections, etc.)

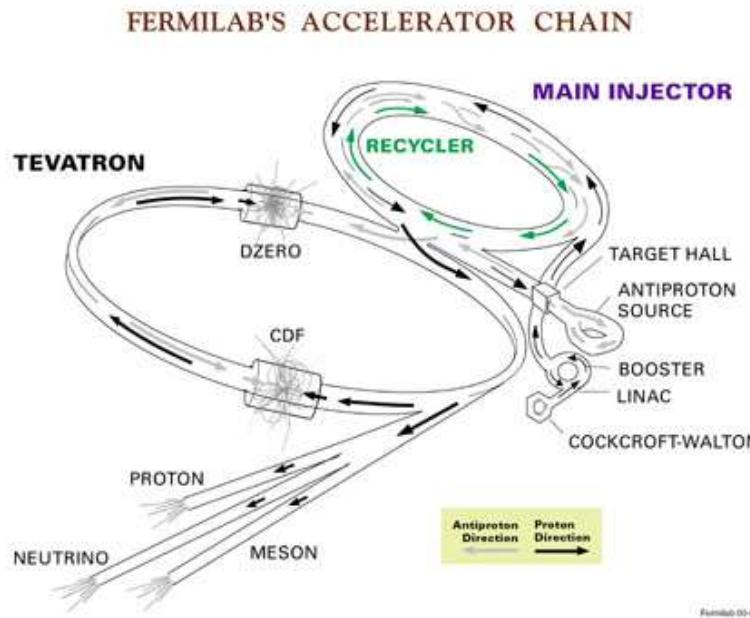
## ⑥ This presentation will focus on $B_s$ system

- △ Mixing:  $\Delta m_s$
- △ Lifetime difference:  $\Delta \Gamma_s$  and  $\phi_s$
- △ Mixing-induced  $CP$  violation:  $A_{SL}^s$
- △ Direct  $CP$  violation:  $A_{CP}(B_s \rightarrow K^- \pi^+)$

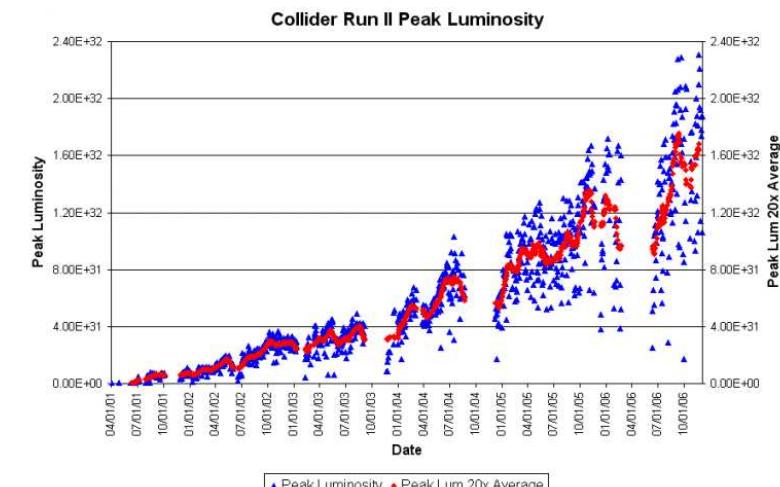
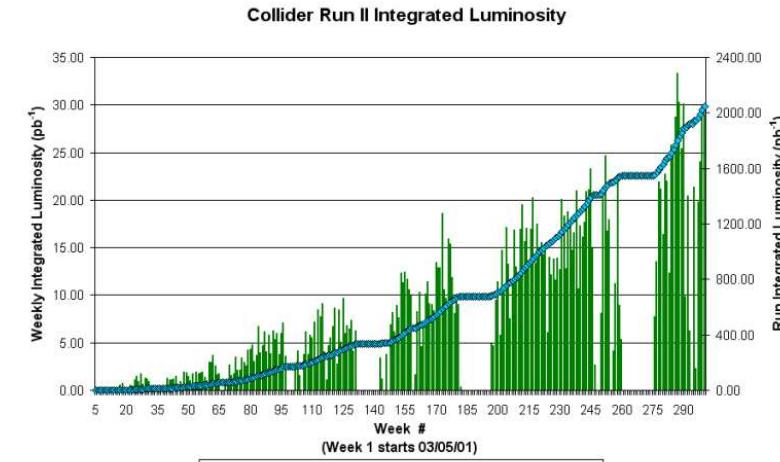
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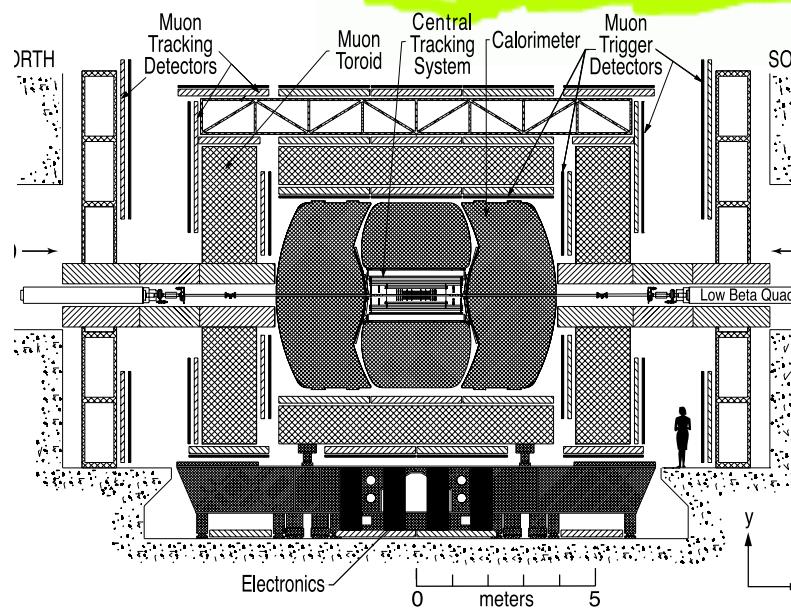
# The Tevatron



- ⑥  $p\bar{p}$  @  $\sqrt{s} = 1.96 \text{ TeV}$
- ⑥  $\sigma(p\bar{p} \rightarrow b\bar{b} + X) \approx 150 \mu\text{b}$
- $B$ -Factories  $\sigma \approx 1 \text{ nb}$
- ⑥ Results:  $\int \mathcal{L} dt = 1 \text{ to } 1.3 \text{ fb}^{-1}$

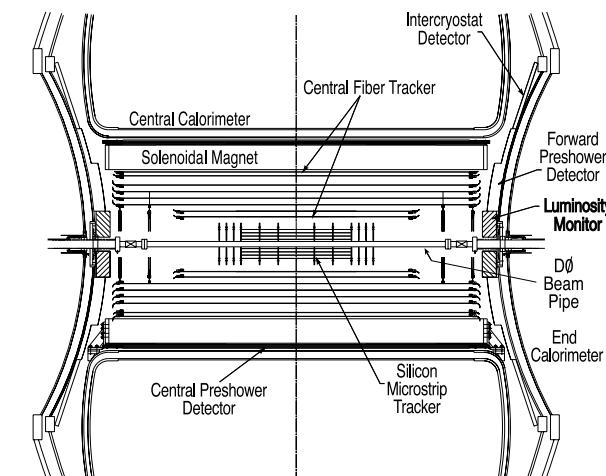


# DØ Detector



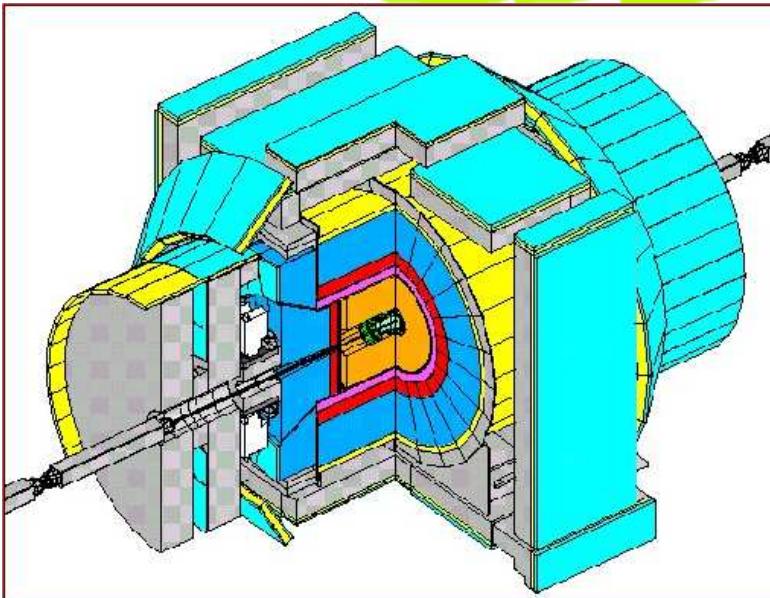
- ➊ Tracker radius: 0.5 m
- ➋ Solenoid  $B$ -Field: 2 T
- ➋ Without L0:  $\delta p_T / p_T = 0.024 p_T$
- ➋ With L0:  $\delta p_T / p_T = 0.0215 p_T$

- ➌ DØ triggers on muons
- ➌ Large muon acceptance
- ➌ Silicon vertex detector—recently added additional inner layer (L0)





# CDF Detector



- ➊ Tracker radius: 1.0 m
- ➋ Solenoid  $B$ -Field: 2 T
- ➌  $p_T$  resolution:  $\frac{\delta p_T}{p_T} = 0.0015 p_T$
- ➍ Particle ID:  $\frac{dE}{dx}$  & TOF

- ➎ Level 1 track trigger
- ➏ Level 2 impact parameter and secondary vertex trigger
- ➐ Trigger on both leptonic and hadronic modes





# The $B_s$ System

- ⌚ Time evolution of  $B_s$  (Flavor Eigenstates)

$$-i \frac{d}{dt} \begin{pmatrix} |B_s^0(t)\rangle \\ |\bar{B}_s^0(t)\rangle \end{pmatrix} = \left( \mathbf{M} + \frac{i}{2} \boldsymbol{\Gamma} \right) \begin{pmatrix} |B_s^0(t)\rangle \\ |\bar{B}_s^0(t)\rangle \end{pmatrix}$$

$CPT \Rightarrow M_{11} = M_{22}$  and  $\Gamma_{11} = \Gamma_{22}$

Hermiticity  $\Rightarrow M_{12} = M_{21}^*$  and  $\Gamma_{12} = \Gamma_{21}^*$

- ⌚ Mass eigenstates (equal  $CP$  eigenstates if  $q/p = 1$ )

$$|B_L\rangle = p|B_s^0\rangle + q|\bar{B}_s^0\rangle$$

$$|B_H\rangle = p|B_s^0\rangle - q|\bar{B}_s^0\rangle$$

$CP$  violation in mixing if  $|q/p| \neq 1$

# Mixing—Overview

- Since Mass and Flavor eigenstates not equal, flavor states can mix.
  - Requires mass of eigenstates to differ ( $\Delta m_q \neq 0$ )
  - Mass eigenstates can have different lifetimes ( $\Delta \Gamma_q \neq 0$ )
  - Standard Model expectation  $\Delta m_q \gg \Delta \Gamma_q$

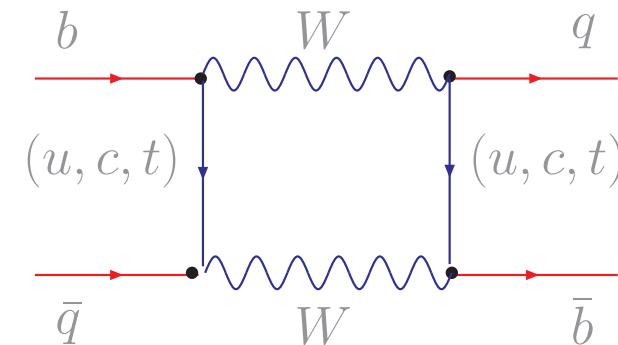
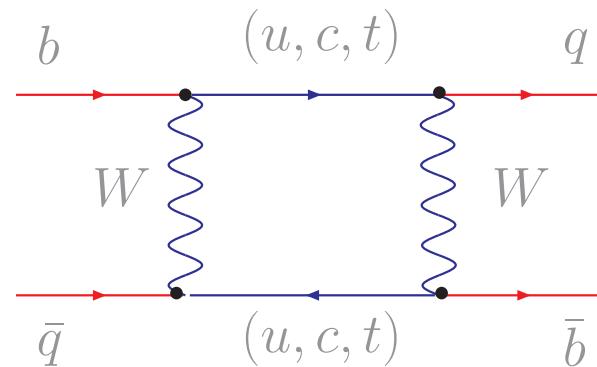
$$\mathcal{P}_{\text{mixed}}^{\text{unmixed}}(t) = \frac{1}{2} \Gamma_q e^{-\frac{\Gamma_q}{2} t} \left[ \cosh \left( \frac{\Delta \Gamma_q}{2} t \right) \pm \cos (\Delta m_q t) \right]$$

where  $\Gamma_q = \frac{\Gamma_H + \Gamma_L}{2}$  the average of the decay widths of the two mass eigenstates.

- Exp. gives  $\Delta \Gamma_q \ll \Delta m_s$  which implies  $|\Gamma_{12}| \ll |M_{12}|$  then  $\Delta m_s \approx 2|M_{12}|$  &  $\Delta \Gamma_s \approx 2|\Gamma_{12}| \cos \phi_s = \Delta \Gamma_{CP} \cos \phi_s$

# Mixing—Overview

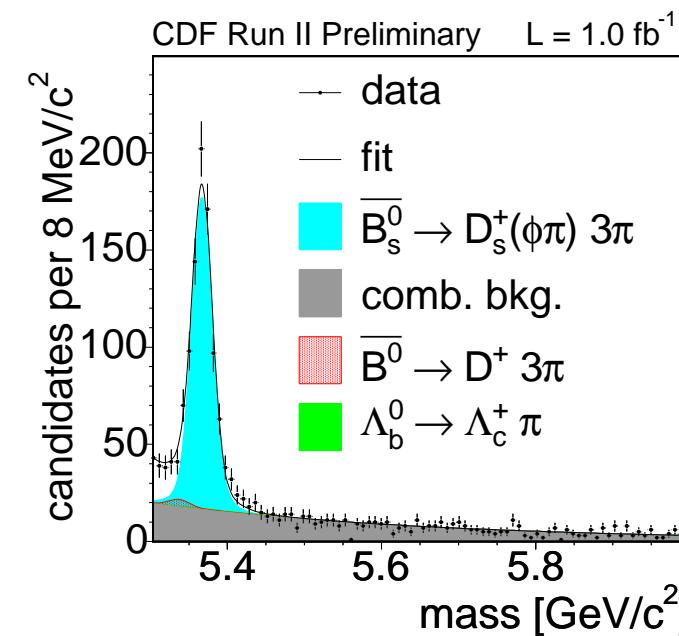
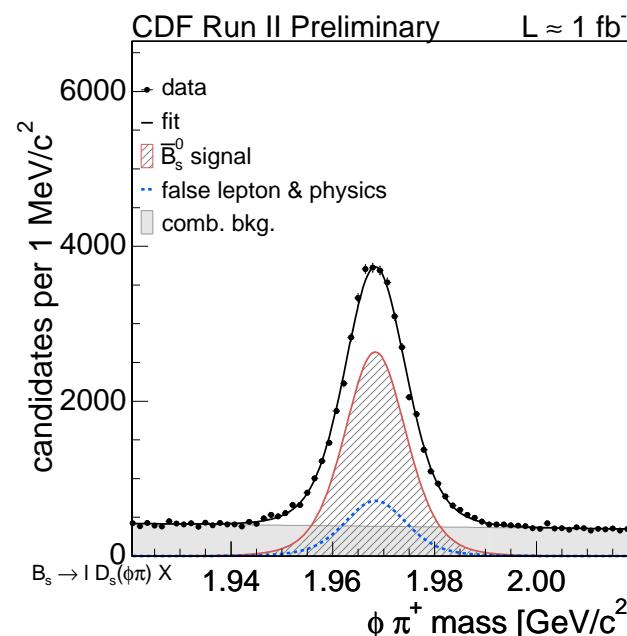
- Mixing requires a  $|\Delta B| = 2$  transition ( $B^0 \rightarrow \bar{B}^0$ )



- Amplitude is  $\propto |V_{tb}V_{tq}|$  because of large  $t$ -quark mass
  - Amplitude  $\propto \sum_q S_0 \left( \frac{m_q}{M_W} \right)$

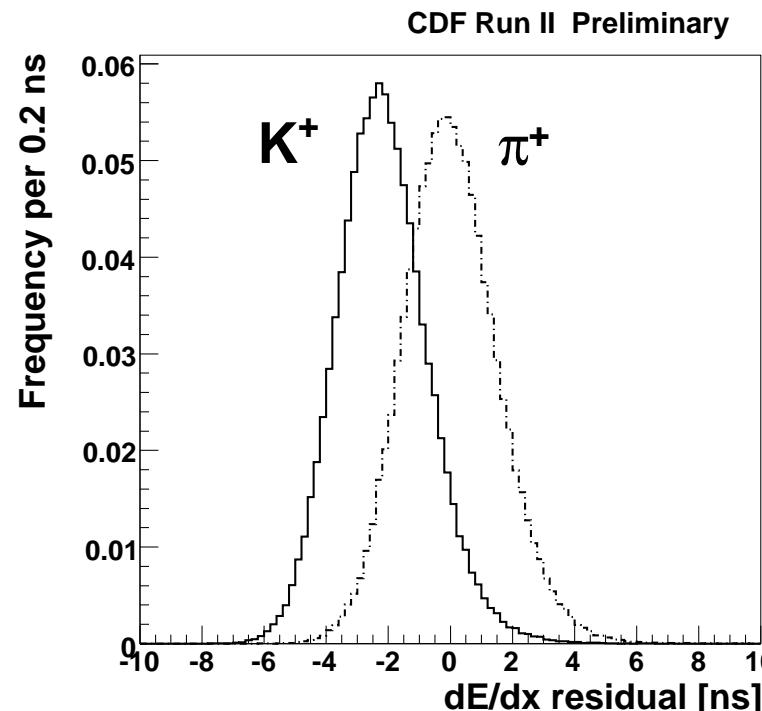
# Mixing—Event Sample

- ⑥ Hadronic (CDF) and Semileptonic (CDF & DØ) samples
  - △ Start by selecting  $D_s^+ \rightarrow \phi(K^+K^-)\pi^+$ ,  $K^{*0}K^+$ ,  $\pi^+\pi^-\pi^+$
- ⑥ Hadronic sample (8700):  $B_s^0 \rightarrow D_s^+\pi^-$ ,  $D_s^+\pi^-\pi^+\pi^-$ 
  - △ Selection uses ANN & kaon-id (TOF &  $dE/dx$ )

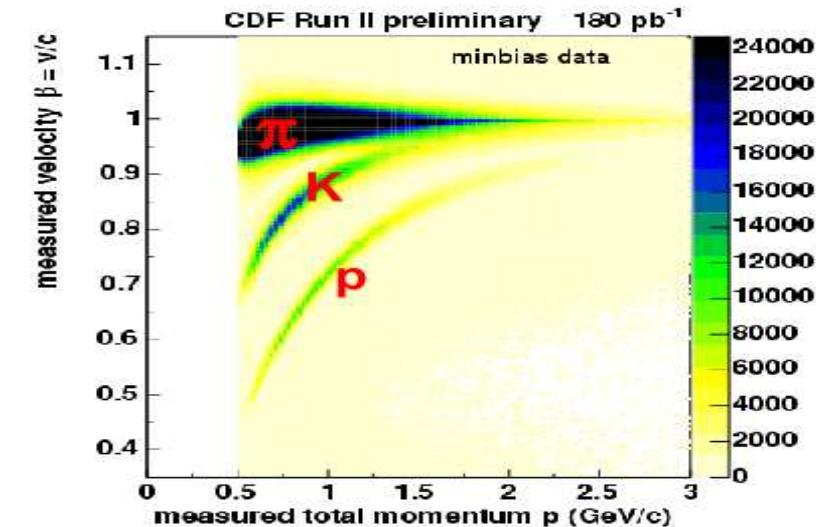


# Mixing—Particle ID

$dE/dx$  in Drift Chamber



Time of Flight (TOF)



$> 1\sigma$   $K/\pi$  Separation up to  $p = 2$  GeV

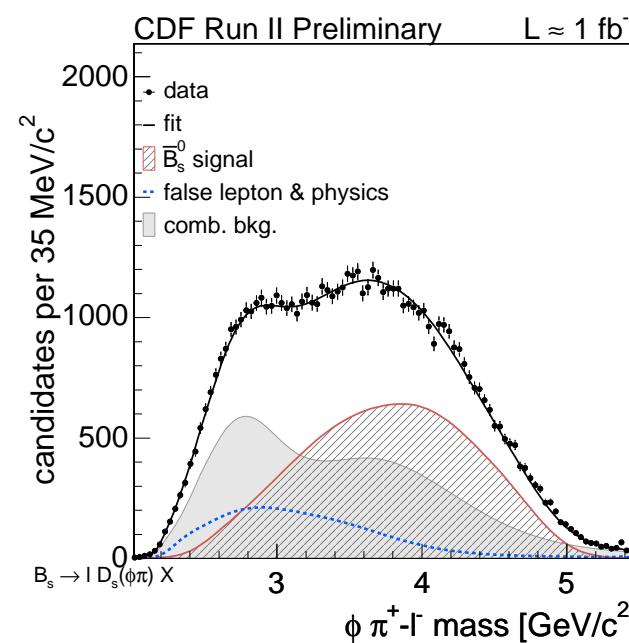
$K/\pi$  separation  $> 1.5\sigma$  @  $p_T > 2$  GeV



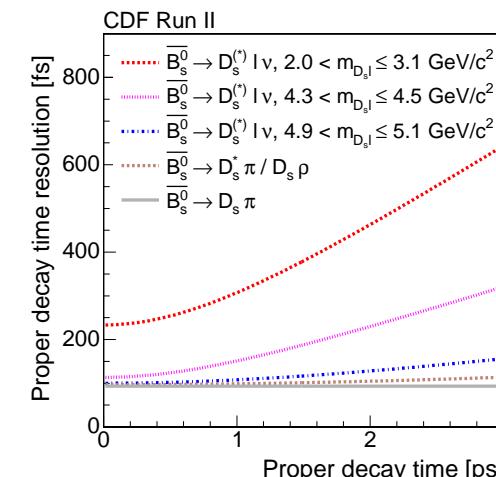
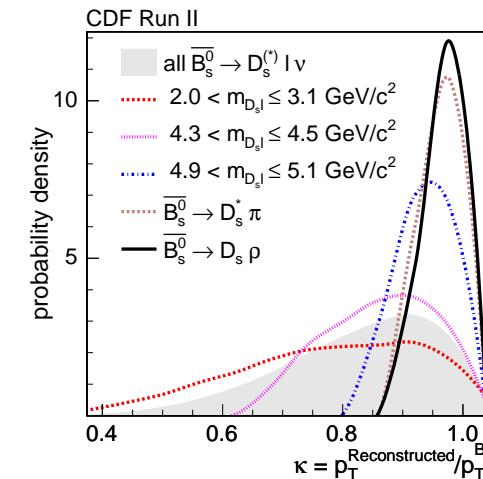
# Mixing—Event Sample

## 6 Semileptonic sample (61500):

$$B_s \rightarrow D_s^+ \ell^- \bar{\nu}_\ell \quad (\ell \text{ is } e \text{ or } \mu)$$



## Semileptonic Lifetime



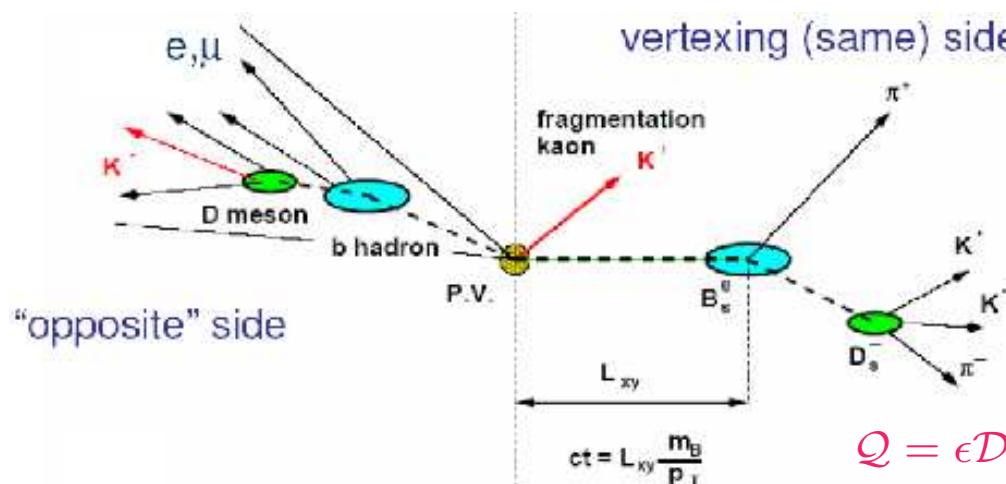
# Mixing—Flavor Tagging

- 6 Mixing requires measurement of initial and final state flavors
  - △ Final state tagging examples

$$B_s^0 \rightarrow D_s^+ \mu^- \nu_\mu$$

$$B_s^0 \rightarrow D_s^+ \pi^-$$

- △ Initial state: opposite or same side charge



Opposite-side Tag (OST):  $K, \ell$ ,  
Jet-charge in NN

Same-side Tag SST:  $K$  in NN

$$\mathcal{Q} = \epsilon \mathcal{D}^2 = \begin{cases} 1.8 \pm 0.1\% & \text{comb. OST} \\ 3.7 \pm 0.9\% & \text{semileptonic SST} \\ 4.8 \pm 1.2\% & \text{hadronic SST} \end{cases}$$

# $B_s$ Mixing—Results

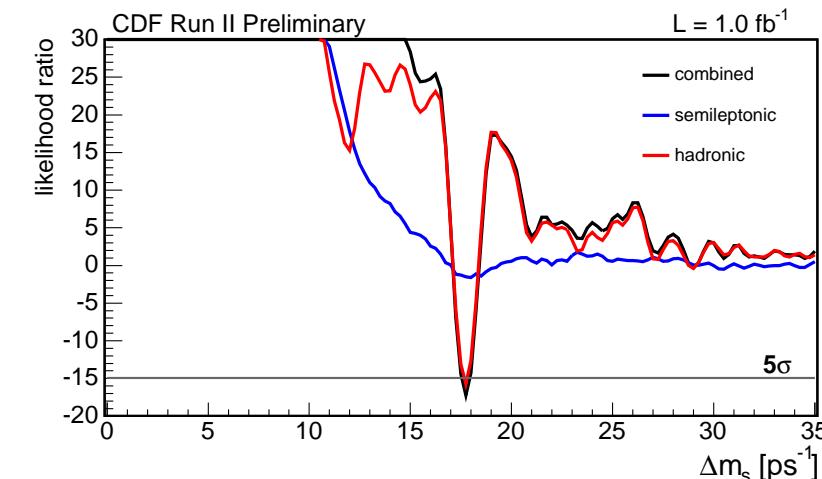
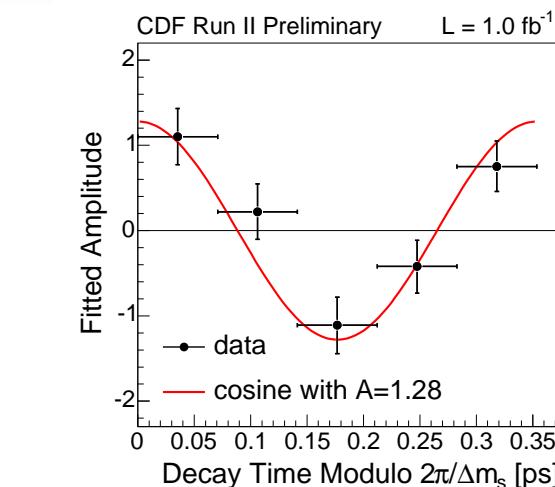
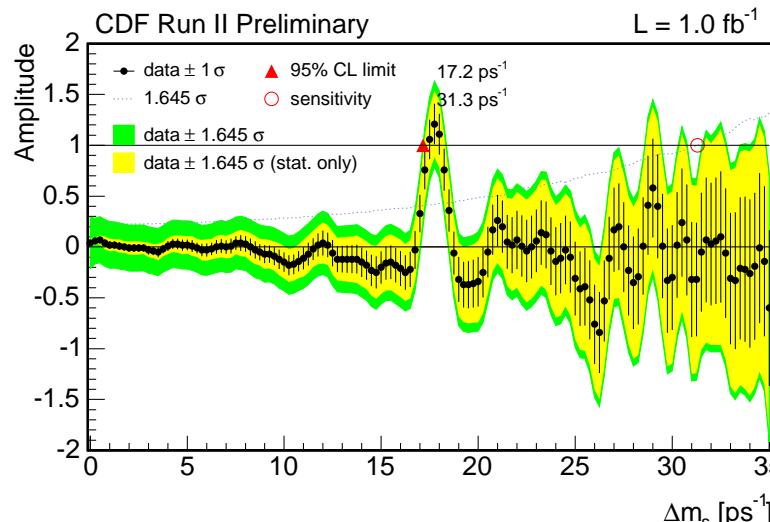
CDF:  $\approx 1 \text{ fb}^{-1}$

$$\Delta m_s = 17.77 \pm 0.10 \pm 0.07 \text{ ps}^{-1}$$

$$|V_{td}/V_{ts}| = 0.2060 \pm 0.0007^{+0.0081}_{-0.0060}$$

DØ:  $\approx 1 \text{ fb}^{-1}$

$17 < \Delta m_s < 21 \text{ ps}^{-1}$  @ 90% CL,  
with  $19 \text{ ps}^{-1}$  most probable value



# $\Delta\Gamma_s$ —Overview

- ⑥ Presentation concentrates on DØ analysis
- ⑥ Lifetime of mass eigenstates not expected to be equal
  - △  $\Delta\Gamma_q/\Gamma_q$  expected to be small, but since  $\Delta m_s \gg \Delta m_d$  might expect  $\Delta\Gamma_s/\Gamma_s \gg \Delta\Gamma_d/\Gamma_d$ 
    - SM predictions:
  - $$\Delta\Gamma_d/\Gamma_d \approx 0.01 \quad \Delta\Gamma_s/\Gamma_s = 0.12 \pm 0.06$$
  - △ Mixing-induced  $CP$  violating phase ( $\Delta\Gamma = \Delta\Gamma_{CP} \cos \phi_s$ ) given by

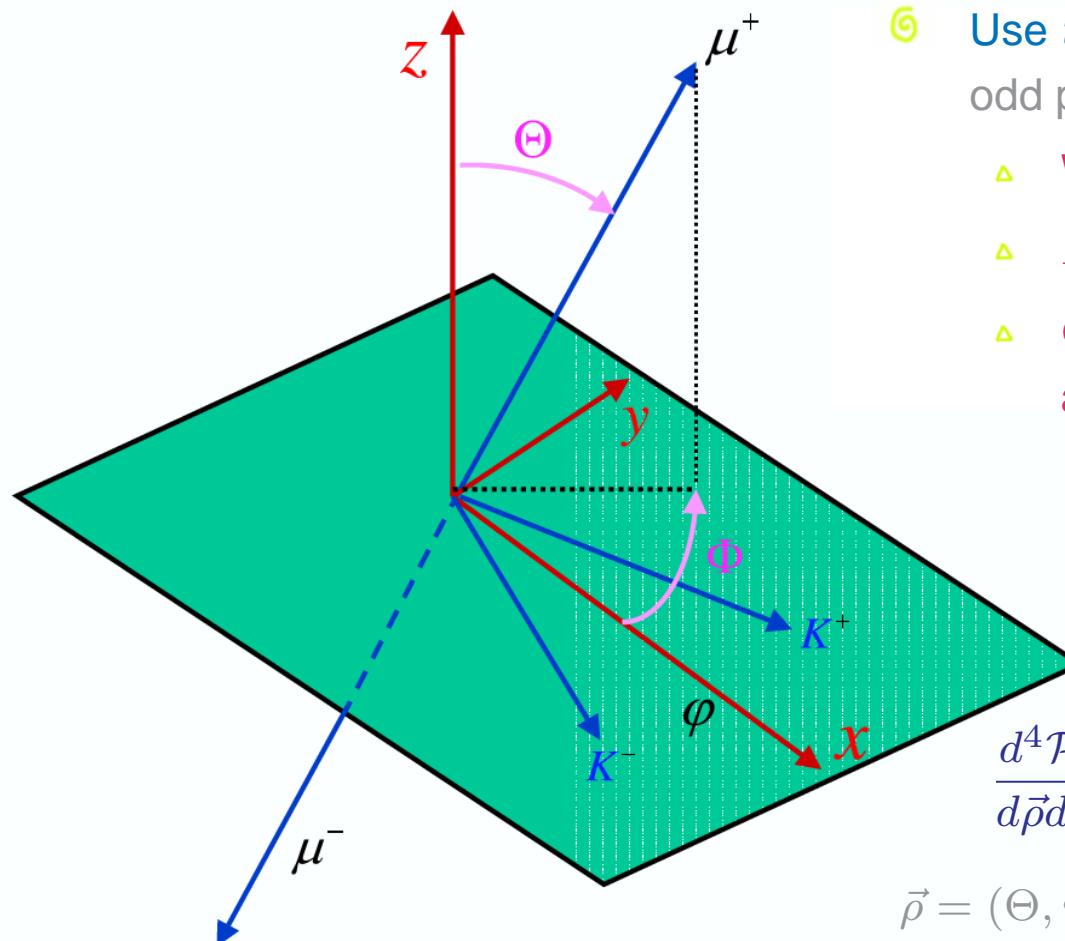
$$e^{i\phi_s} = \frac{V_{ts} V_{tb}^*}{V_{ts}^* V_{tb}} \frac{V_{cs}^* V_{cb}}{V_{cs} V_{cb}^*} \quad \Rightarrow \quad \phi_s \approx -0.03$$

## $\Delta\Gamma_s$ —Analysis

- ⑥ Must separate the two mass eigenstates
  - △ These are the  $CP$  even and odd states for small  $\phi_s$
  - $$B_s^H = \frac{1}{\sqrt{2}} [ |B_s\rangle + |\bar{B}_s\rangle ] \quad CP \text{ odd}$$
  - $$B_s^L = \frac{1}{\sqrt{2}} [ |B_s\rangle - |\bar{B}_s\rangle ] \quad CP \text{ even}$$
  - △ Use  $B_s \rightarrow J/\psi\phi$  w/final state  $J = 0$  since  $J/\psi$  &  $\phi$  have  $S = 1$  this  $\Rightarrow \ell = 0, 1, 2$  ( $S, P, D$  wave)
    - △  $S$  &  $D \Rightarrow CP$  even
    - △  $P \Rightarrow CP$  odd
- ⑥ Goal is to disentangle different  $\ell$  states

# $\Delta\Gamma_s$ Analysis

## Transversity Angles



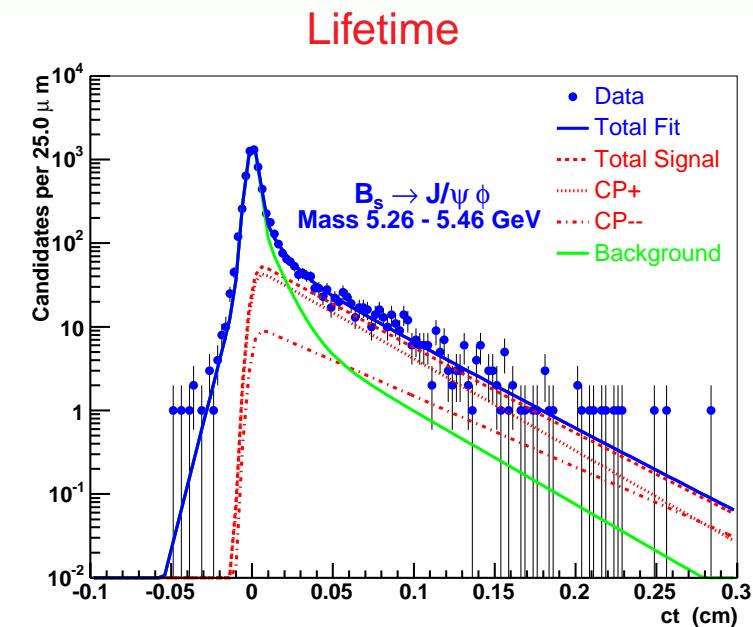
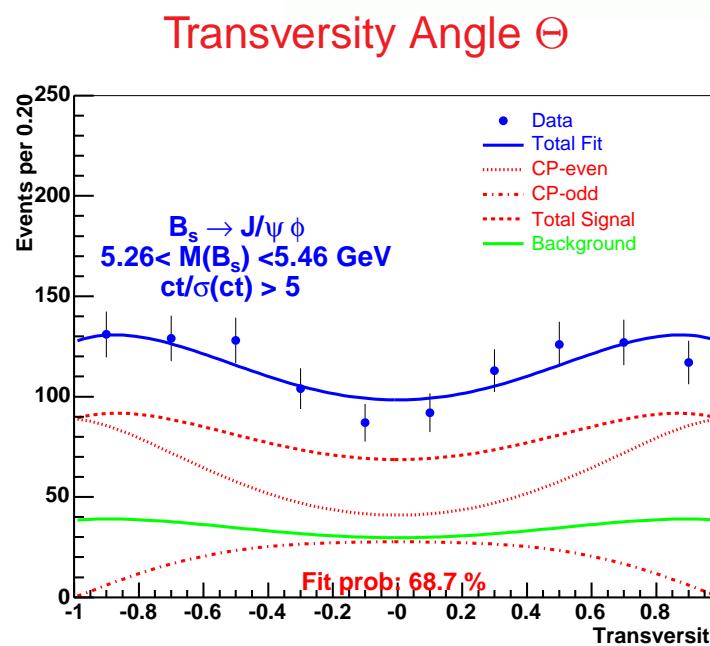
- ➊ Use  $B_s \rightarrow J/\psi\phi$
- ➋ Use *transversity angles*—Separates odd parity states nicely
  - △ Work in  $J/\psi$  rest frame
  - △  $K^+ K^-$  defines  $x-y$  plane
  - △  $\Theta, \Phi$  are  $\mu^+$  polar, azimuthal angles,  $\Psi$  helicity angle of  $K^+$

Angular Distribution  $B_s$

$$\frac{d^4\mathcal{P}}{d\vec{p}dt} \propto f(\vec{\rho}, t; A_0, A_\perp, A_\parallel, \delta_1, \delta_2, \phi_s)$$

$$\vec{\rho} = (\Theta, \Phi, \Psi)$$

# $\Delta\Gamma_s$ Analysis



## DØ Results

$$\phi_s = -0.79 \pm 0.56 \pm 0.01 \text{ Fit}$$

$$\Delta\Gamma_s = 0.17 \pm 0.09 \pm 0.03 \text{ ps}^{-1}$$

$$\bar{\tau} = 1.49 \pm 0.08^{+0.01}_{-0.03} \text{ ps}$$

$$\phi_s = 0 \text{ Fixed}$$

$$\Delta\Gamma_s = 0.12 \pm 0.08^{+0.03}_{-0.04} \text{ ps}^{-1}$$

$$\bar{\tau} = 1.52 \pm 0.08^{+0.01}_{-0.04} \text{ ps}$$

# *CP Asymmetry*

- ⑥ DØ measurement of mixing-induced *CP* asymmetry  $A_{SL}$  and phase  $\phi_s$  —Flavor specific final states.

- △ Measure untagged time-integrated muon asymmetry
  - △ Exclusive mode  $B_s \rightarrow D_s^- (\phi \pi^-) \mu^+ \nu X$

$$\frac{N(D_s \mu^+) - N(D_s \mu^-)}{N(D_s \mu^+) + N(D_s \mu^-)} = A_{SL}^s = \frac{\Delta \Gamma_s}{\Delta m_s} \tan \phi_s$$

- △ Inclusive mode  $p\bar{p} \rightarrow \mu^\pm \mu^\pm$  (Like-sign asymmetry)

$$\frac{N(\mu^+ \mu^+) - N(\mu^- \mu^-)}{N(\mu^+ \mu^+) + N(\mu^- \mu^-)} = 2A_{SL}(\text{untagged})$$

- ⑥ Both measurements use similar analysis methods



## *CP Asymmetry*



- ➄ Systematics: Various detector & physics processes can cause an asymmetry.

- △ Data split into 8 sample: split by sign of charge ( $q$ ), rapidity ( $\gamma$ ), toroid polarity ( $\beta$ )
  - △ Fit eight functions for 8 parameters

$$n_q^{\beta\gamma} = \frac{1}{4} N \epsilon^\beta (1 + qA)(1 + q\gamma A_{fb})(1 + \gamma A_{det}) \\ \times (1 + q\beta\gamma A_{ro})(1 + q\beta A_{q\beta})(1 + \beta\gamma A_{\beta\gamma})$$

$n_q^{\beta\gamma}$ : number of events in sample (given)

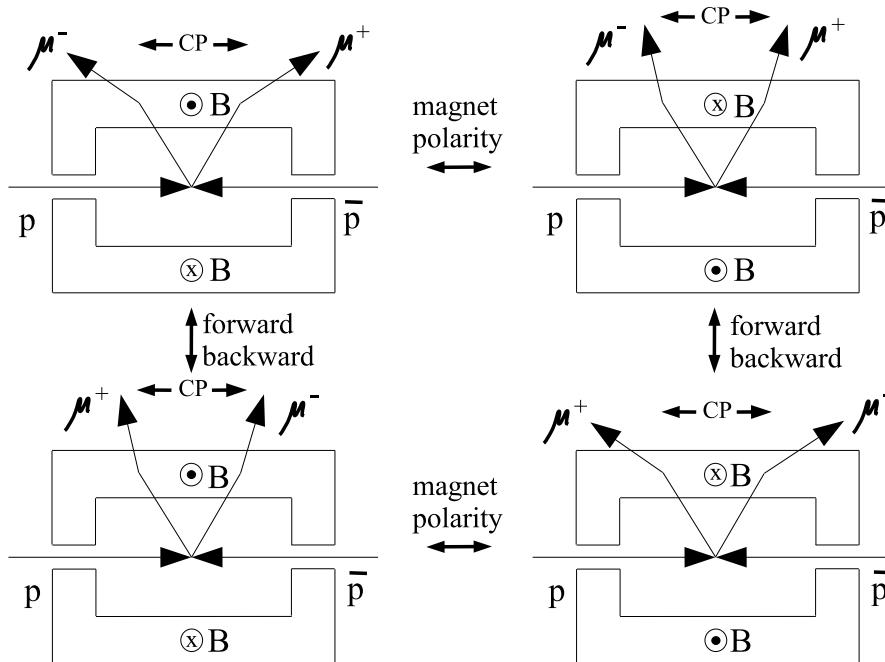
$A$ : asymmetry from  $CP$  violation in  $B_s$  mixing

$A_{xx}$ : detector and beam asymmetries



## Detector Asymmetries—Examples

- Asymmetry w/toroid polarity  $\beta$ :  $A^\beta = A + \beta A_{q\beta}$  (first order)
- Beam & detector asymmetries:  $f(n_q^{\beta\gamma}) = A + A_{fb}A_{det}$  (second order)



$A_{ro}$ : Change in detector acceptance and range out of muons in bending toward (away) from beamline

# CP Asymmetry—Results

- Inclusive mode  $p\bar{p} \rightarrow \mu^\pm \mu^\pm$  (Like-sign asymmetry)

$$\left. \begin{array}{l} A = -0.0005 \pm 0.0013 \\ \delta A = -0.0023 \pm 0.0008 \end{array} \right\} \Rightarrow A_{SL} = -0.0028 \pm 0.0013 \pm 0.0009$$

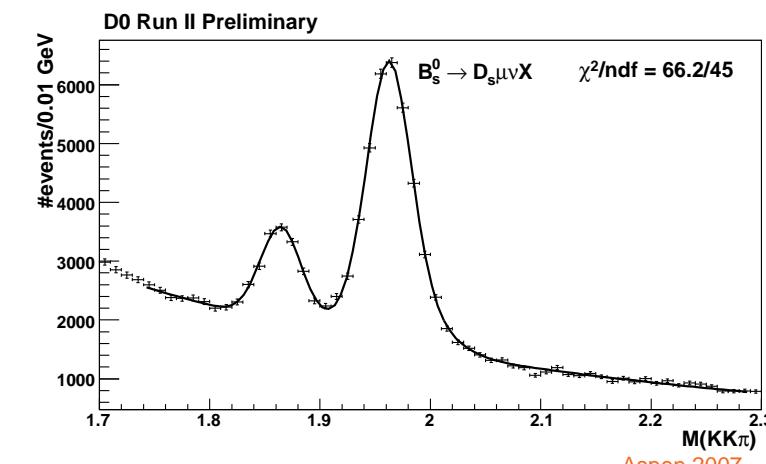
Combine with  $B$ -Factories to extract  $A_{SL}^s$

$\delta A$  asymmetry from  $K^\pm$  decays:  $K^+N \rightarrow$  hyperon, does not exist for  $K^-$ .

- Exclusive mode  $B_s \rightarrow D_s^-(\phi\pi^-)\mu^+\nu X$

$$A_{SL}^s = 0.0245 \pm 0.0193 \pm 0.0035$$

Combine with  $\Delta\Gamma_s$  and  $\Delta m_s$  to extract  $\phi_s$ .



# Direct $CP$ Violation

- ⑥ CDF measures  $B_{(s)} \rightarrow hh'$  (recent result on  $B_{(s)} \rightarrow K^-\pi^+$ )
- ⑥ Standard Model predicts for  $B_{(s)} \rightarrow K^-\pi^+$

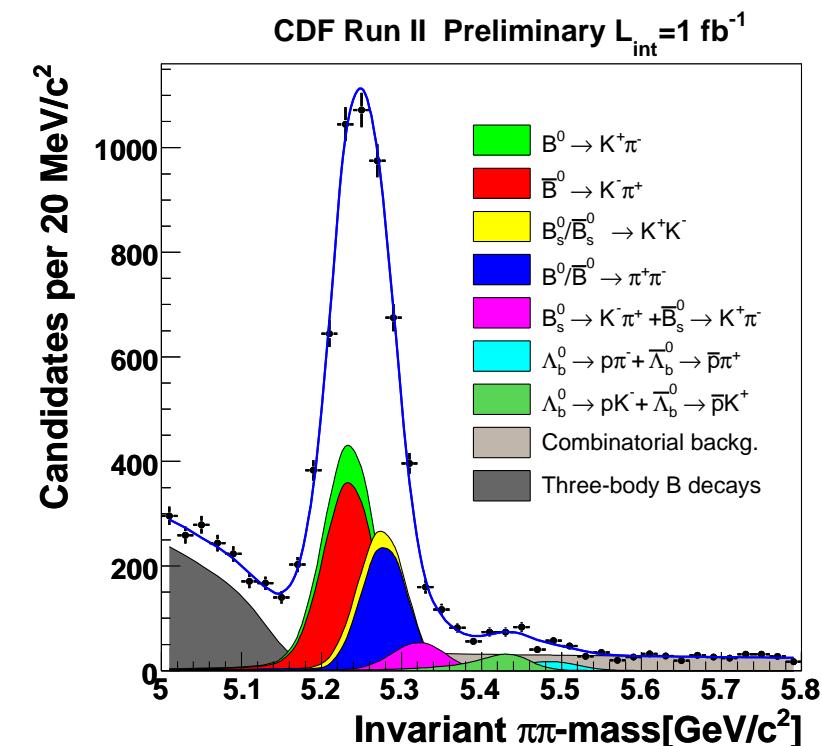
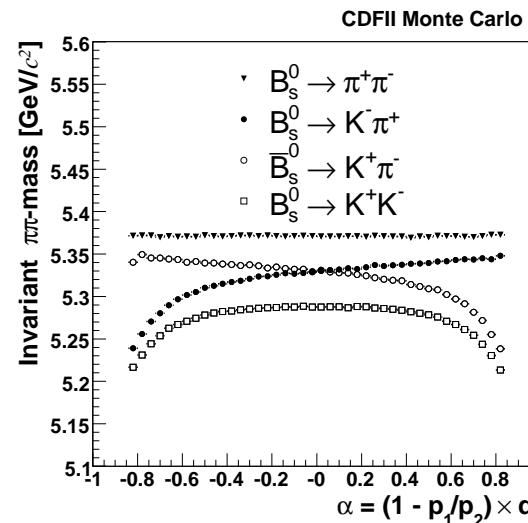
$$|A(B_s \rightarrow \pi^+ K^-)|^2 - |A(\bar{B}_s \rightarrow \pi^- K^+)|^2 \\ = |A(\bar{B}_d \rightarrow \pi^+ K^-)|^2 - |A(B_d \rightarrow \pi^- K^+)|^2$$

Direct  $CP$  violation in  $B_d$  measured by BaBar, Belle, CDF

- △ Direct  $CP$  violation requires amplitudes with different strong and weak phases (this mode dominated by penguin diagram)
- △ Expected only in the SM (new physics would have hard time accommodating this result)
- ⑥ Asymmetry can be used to measure CKM angle  $\gamma$

# Direct CP Violation

- ⑥ Trigger on pair of opposite charge tracks with displaced vertex
- ⑥ Impose isolation
- ⑥ Assume tracks are pions
- ⑥ Likelihood to separate modes (Includes particle ID,  $p_{tot}$ ,  $M_{ij}$ , signed momentum imbalance ( $\alpha$ ))



Correction for difference in  $K^+$   $K^-$  interaction in material

# Direct CP Violation

- First observation of  $B_s \rightarrow \pi^+ K^-$  with significance of  $8.2\sigma$
- $A_{CP}(B_s \rightarrow \pi^+ K^-) = 0.39 \pm 0.15 \pm 0.08$ 
  - Comparison to  $B_d$  —consistent with SM

$$\frac{|A(\bar{B}_d \rightarrow \pi^+ K^-)|^2 - |A(B_d \rightarrow \pi^- K^+)|^2}{|A(B_s \rightarrow \pi^+ K^-)|^2 - |A(\bar{B}_s \rightarrow \pi^- K^+)|^2} = 0.84 \pm 0.42 \pm 0.15$$

$B_d$  previously measured by BaBar, Belle, CDF

- Branching ratio  $\mathcal{B}(B_s^0 \rightarrow K^- \pi^+) = (5.0 \pm 0.75 \pm 0.36) \times 10^{-6}$   
SM Prediction:  $\mathcal{B}(B_s^0 \rightarrow K^- \pi^+) = 4.9 \times 10^{-6}$   
World average:  $\mathcal{B}(B_d^0 \rightarrow K^+ \pi^-) = (19.7 \pm 0.6) \times 10^{-6}$

# Summary

This talk has concentrated on  $B_s$  decays, but the Tevatron has produced a large number of other  $B$ -physics results.

- ⑥ CDF measures  $B_s^0$ - $\bar{B}_s^0$ 
  - △  $\Delta m_s = 17.77 \pm 0.10 \pm 0.07 \text{ ps}^{-1}$
- ⑥ DØ measures  $\Delta\Gamma_s$  and  $\phi_s$ 
  - △  $\Delta\Gamma_s = 0.17 \pm 0.09 \pm 0.03 \text{ ps}^{-1}$  &  $\phi_s = -0.79 \pm 0.56 \pm 0.01$
- ⑥ DØ measures semileptonic decay asymmetry
  - △ Exclusive mode:  $A_{SL}^s = 0.0245 \pm 0.0193 \pm 0.0035$
  - △ Inclusive mode:  $A_{SL} = -0.0028 \pm 0.0013 \pm 0.0009$
- ⑥ CDF measures direct  $CP$  violation in  $B_s \rightarrow K^- \pi^+$ 
  - △  $A_{CP}(B_s \rightarrow \pi^+ K^-) = 0.39 \pm 0.15 \pm 0.08$